Model-Based RL and Policy Learning

CS 294-112: Deep Reinforcement Learning

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Overview

- 1. Last time: learning models of system dynamics and using optimal control to choose actions
 - Global models and model-based RL
 - Local models and model-based RL with *constraints*
- 2. What if we want a *policy*?
 - Much quicker to evaluate actions at runtime
 - Potentially better generalization
- 3. Can we just backpropagate into the policy?

Today's Lecture

- 1. Backpropagating into a policy with learned models
- 2. How this becomes equivalent to *imitating* optimal control
- 3. The guided policy search algorithm
- 4. Imitating optimal control with DAgger
- 5. Model-based vs. model-free RL tradeoffs
- Goals
 - Understand how to train policies using optimal control
 - Understand tradeoffs between various methods

So how can we train policies?

- So far we saw how we can...
 - Train global models (e.g. GPs, neural networks)
 - Train local models (e.g. linear models)
 - Combine global and local models (e.g. using Bayesian linear regression)
- But what if we want a policy?
 - Don't need to replan (faster)
 - Potentially better generalization





Backpropagate directly into the policy?



easy for deterministic policies, but also possible for stochastic policy

model-based reinforcement learning version 2.0:

- 1. run base policy $\pi_0(\mathbf{u}_t|\mathbf{x}_t)$ (e.g., random policy) to collect $\mathcal{D} = \{(\mathbf{x}, \mathbf{u}, \mathbf{x}')_i\}$
- 2. learn dynamics model $f(\mathbf{x}, \mathbf{u})$ to minimize $\sum_i ||f(\mathbf{x}_i, \mathbf{u}_i) \mathbf{x}'_i||^2$
- 3. backpropagate through $f(\mathbf{x}, \mathbf{u})$ into the policy to optimize $\pi_{\theta}(\mathbf{u}_t | \mathbf{x}_t)$
- 4. run $\pi_{\theta}(\mathbf{u}_t | \mathbf{x}_t)$, appending the visited tuples $(\mathbf{x}, \mathbf{u}, \mathbf{x}')$ to \mathcal{D}

What's the problem with backprop into policy?









- Similar parameter sensitivity problems as shooting methods
 - But no longer have convenient second order LQR-like method, because policy parameters couple all the time steps, so no dynamic programming
- Similar problems to training long RNNs with BPTT
 - Vanishing and exploding gradients
 - Unlike LSTM, we can't just "choose" a simple dynamics, dynamics are chosen by nature

• What about collocation methods?

$$\min_{\mathbf{u}_1,\ldots,\mathbf{u}_T,\mathbf{x}_1,\ldots,\mathbf{x}_T} \sum_{t=1}^T c(\mathbf{x}_t,\mathbf{u}_t) \text{ s.t. } \mathbf{x}_t = f(\mathbf{x}_{t-1},\mathbf{u}_{t-1})$$



• What about collocation methods?

$$\min_{\mathbf{u}_1,\ldots,\mathbf{u}_T,\mathbf{x}_1,\ldots,\mathbf{x}_T,\theta} \sum_{t=1}^T c(\mathbf{x}_t,\mathbf{u}_t) \text{ s.t. } \mathbf{x}_t = f(\mathbf{x}_{t-1},\mathbf{u}_{t-1}), \mathbf{u}_t = \pi_{\theta}(\mathbf{x}_t)$$



Even simpler...

$$\min_{\mathbf{u}_1,\ldots,\mathbf{u}_T,\mathbf{x}_1,\ldots,\mathbf{x}_T,\theta} \sum_{t=1}^T c(\mathbf{x}_t,\mathbf{u}_t) \text{ s.t. } \mathbf{x}_t = f(\mathbf{x}_{t-1},\mathbf{u}_{t-1}) \int_{\mathsf{however you want}}^{\mathsf{generic trajectory}} \mathsf{generic trajectory} \mathsf{optimization, solve} \mathsf{however you want}$$

s.t. $\mathbf{u}_t = \pi_{\theta}(\mathbf{x}_t)$

• How can we impose constraints on trajectory optimization?

Review: dual gradient descent

$$\min_{\mathbf{x}} f(\mathbf{x}) \text{ s.t. } C(\mathbf{x}) = 0$$

$$\mathcal{L}(\mathbf{x},\lambda) = f(\mathbf{x}) + \lambda C(\mathbf{x})$$

$$g(\lambda) = \mathcal{L}(\mathbf{x}^{\star}(\lambda), \lambda)$$

$$\mathbf{x}^{\star} = \arg\min_{\mathbf{x}} \mathcal{L}(\mathbf{x}, \lambda)$$

$$\frac{dg}{d\lambda} = \frac{d\mathcal{L}}{d\lambda}(\mathbf{x}^{\star}, \lambda)$$

1. Find $\mathbf{x}^{\star} \leftarrow \arg \min_{\mathbf{x}} \mathcal{L}(\mathbf{x}, \lambda)$ 2. Compute $\frac{dg}{d\lambda} = \frac{d\mathcal{L}}{d\lambda}(\mathbf{x}^{\star}, \lambda)$ 3. $\lambda \leftarrow \lambda + \alpha \frac{dg}{d\lambda}$

A small tweak to DGD: augmented Lagrangian

n (

$$\min_{\mathbf{x}} f(\mathbf{x}) \text{ s.t. } C(\mathbf{x}) = 0$$

$$\mathcal{L}(\mathbf{x}, \lambda) = f(\mathbf{x}) + \lambda C(\mathbf{x})$$
$$\bar{\mathcal{L}}(\mathbf{x}, \lambda) = f(\mathbf{x}) + \lambda C(\mathbf{x}) + \rho \|C(\mathbf{x})\|^2$$

()

- Still converges to correct solution
- When far from solution, quadratic term tends to improve stability
- Closely related to alternating direction method of multipliers (ADMM)

1. Find $\mathbf{x}^* \leftarrow \arg\min_{\mathbf{x}} \bar{\mathcal{L}}(\mathbf{x}, \lambda)$ 2. Compute $\frac{dg}{d\lambda} = \frac{d\bar{\mathcal{L}}}{d\lambda}(\mathbf{x}^*, \lambda)$ 3. $\lambda \leftarrow \lambda + \alpha \frac{dg}{d\lambda}$

Constraining trajectory optimization with dual gradient descent

 $\min_{\tau,\theta} c(\tau) \text{ s.t. } \mathbf{u}_t = \pi_{\theta}(\mathbf{x}_t)$

$$\mathcal{L}(\tau, \theta, \lambda) = c(\tau) + \sum_{t=1}^{T} \lambda_t(\pi_\theta(\mathbf{x}_t) - \mathbf{u}_t)$$

$$\bar{\mathcal{L}}(\tau,\theta,\lambda) = c(\tau) + \sum_{t=1}^{T} \lambda_t (\pi_\theta(\mathbf{x}_t) - \mathbf{u}_t) + \sum_{t=1}^{T} \rho_t (\pi_\theta(\mathbf{x}_t) - \mathbf{u}_t)^2$$

Constraining trajectory optimization with dual gradient descent

$$\min_{\tau,\theta} c(\tau) \text{ s.t. } \mathbf{u}_t = \pi_{\theta}(\mathbf{x}_t)$$
$$\bar{\mathcal{L}}(\tau,\theta,\lambda) = c(\tau) + \sum_{t=1}^T \lambda_t (\pi_{\theta}(\mathbf{x}_t) - \mathbf{u}_t) + \sum_{t=1}^T \rho_t (\pi_{\theta}(\mathbf{x}_t) - \mathbf{u}_t)^2$$

1. Find
$$\tau \leftarrow \arg \min_{\tau} \bar{\mathcal{L}}(\tau, \theta, \lambda)$$
 (e.g. via iLQR)
2. Find $\theta \leftarrow \arg \min_{\theta} \bar{\mathcal{L}}(\tau, \theta, \lambda)$ (e.g. via SGD)
3. $\lambda \leftarrow \lambda + \alpha \frac{dg}{d\lambda}$

Guided policy search discussion

1. Find
$$\tau \leftarrow \arg \min_{\tau} \bar{\mathcal{L}}(\tau, \theta, \lambda)$$
 (e.g. via iLQR)
2. Find $\theta \leftarrow \arg \min_{\theta} \bar{\mathcal{L}}(\tau, \theta, \lambda)$ (e.g. via SGD)
3. $\lambda \leftarrow \lambda + \alpha \frac{dg}{d\lambda}$

- Can be interpreted as constrained trajectory optimization method
- Can be interpreted as imitation of an optimal control expert, since step 2 is just supervised learning
- The optimal control "teacher" adapts to the learner, and avoids actions that the learner can't mimic

General guided policy search scheme

- \rightarrow 1. Optimize $p(\tau)$ with respect to some surrogate $\tilde{c}(\mathbf{x}_t, \mathbf{u}_t)$
 - 2. Optimize θ with respect to some supervised objective
- = 3. Increment or modify dual variables λ

Need to choose:

form of $p(\tau)$ optimization method for $p(\tau)$ surrogate $\tilde{c}(\mathbf{x}_t, \mathbf{u}_t)$ supervised objective for $\pi_{\theta}(\mathbf{u}_t | \mathbf{x}_t)$

Deterministic case



- \rightarrow 1. Optimize τ with respect to surrogate $\tilde{c}(\tau)$
 - 2. Optimize θ with respect to supervised objective
 - **3**. Increment or modify dual variables λ

Learning with multiple trajectories



1. Optimize each τ_i in parallel with respect to c̃(τ_i)
2. Optimize θ with respect to supervised objective
3. Increment or modify dual variables λ

Case study: learning locomotion skills

Interactive Control of Diverse Complex Characters with Neural Networks

Igor Mordatch, Kendall Lowrey, Galen Andrew, Zoran Popovic, Emanuel Todorov Department of Computer Science, University of Washington {mordatch, lowrey, galen, zoran, todorov}@cs.washington.edu

Interactive Control of Diverse Complex Characters with Neural Networks

Submitted to NIPS 2015

Stochastic (Gaussian) GPS

$$\min_{p,\theta} E_{\tau \sim p(\tau)}[c(\tau)] \text{ s.t. } p(\mathbf{u}_t | \mathbf{x}_t) = \pi_{\theta}(\mathbf{u}_t | \mathbf{x}_t)$$

$$p(\mathbf{u}_t | \mathbf{x}_t) = \mathcal{N}(\mathbf{K}_t(\mathbf{x}_t - \hat{\mathbf{x}}_t) + \mathbf{k}_t + \hat{\mathbf{u}}_t, \Sigma_t)$$

$$\int \cdots \sum_{p} \sum_{t=1}^T E_{p(\mathbf{x}_t, \mathbf{u}_t)} [\tilde{c}(\mathbf{x}_t, \mathbf{u}_t)] \text{ s.t. } D_{\mathrm{KL}}(p(\tau) || \bar{p}(\tau)) \leq \epsilon$$

▶ 1. Optimize $p(\tau)$ with respect to some surrogate $\tilde{c}(\mathbf{x}_t, \mathbf{u}_t)$

- 2. Optimize θ with respect to some supervised objective
- **3**. Increment or modify dual variables λ

Stochastic (Gaussian) GPS with local models



Robotics Example



Input Remapping Trick

 $\min_{p,\theta} E_{\tau \sim p(\tau)}[c(\tau)] \text{ s.t. } p(\mathbf{u}_t | \mathbf{x}_t) = \pi_{\theta}(\mathbf{u}_t | \mathbf{z}_t)$ training time test time





CNN Vision-Based Policy



Case study: vision-based control with GPS

End-to-End Training of Deep Visuomotor Policies

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Case study: vision-based control with GPS

Learned Visuomotor Policy: Shape sorting cube

Break

Imitating optimal control with DAgger

Deep Learning for Real-Time Atari Game Play Using Offline Monte-Carlo Tree Search Planning

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A problem with DAgger

- $\rightarrow 1$. train $\pi_{\theta}(\mathbf{u}_t | \mathbf{o}_t)$ from human data $\mathcal{D} = \{\mathbf{o}_1, \mathbf{u}_1, \dots, \mathbf{o}_N, \mathbf{u}_N\}$
 - 2. run $\pi_{\theta}(\mathbf{u}_t | \mathbf{o}_t)$ to get dataset $\mathcal{D}_{\pi} = \{\mathbf{o}_1, \dots, \mathbf{o}_M\}$
 - 3. Ask hommanteo tobleb $\mathcal{D}_{\pi}\mathcal{D}_{\mathcal{H}}$ ithitactions \mathbf{u}_t
- 4. Aggregate: $\mathcal{D} \leftarrow \mathcal{D} \cup \mathcal{D}_{\pi}$



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 - 4. Aggregate: $\mathcal{D} \leftarrow \mathcal{D} \cup \mathcal{D}_{\pi}$

simple stochastic policy: $\hat{\pi}(\mathbf{u}_t | \mathbf{x}_t) = \mathcal{N}(\mathbf{K}_t \mathbf{x}_t + \mathbf{k}_t, \Sigma_{\mathbf{u}_t})$

$$\hat{\pi}(\mathbf{u}_t|\mathbf{x}_t) = \arg\min_{\hat{\pi}} \sum_{t'=t}^T E_{\hat{\pi}}[c(\mathbf{x}_{t'}, \mathbf{u}_{t'})] + \lambda D_{\mathrm{KL}}(\hat{\pi}(\mathbf{u}_t|\mathbf{x}_t) || \pi_{\theta}(\mathbf{u}_t|\mathbf{o}_t))$$



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$$\pi_{\theta}(\mathbf{u}_2 | \mathbf{o}_2)$$
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replanning = \mathbf{M} odel \mathbf{P} redictive \mathbf{C} ontrol (MPC)

 $\pi_{\theta}(\mathbf{u}_t | \mathbf{o}_t)$ – control from **images** $\hat{\pi}(\mathbf{u}_t | \mathbf{x}_t)$ – control from **states**



- 1. train $\pi_{\theta}(\mathbf{u}_t | \mathbf{o}_t)$ from human data $\mathcal{D} = \{\mathbf{o}_1, \mathbf{u}_1, \dots, \mathbf{o}_N, \mathbf{u}_N\}$ 2. run $\hat{\pi}(\mathbf{u}_t | \mathbf{o}_t)$ to get dataset $\mathcal{D}_{\pi} = \{\mathbf{o}_1, \dots, \mathbf{o}_M\}$ 3. Ask computer to label \mathcal{D}_{π} with actions \mathbf{u}_t
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 $\mathbf{v}_{t'=t} = \mathbf{v}_{t'=t} = \mathbf{v}_{t'=t} \sum_{t'=t}^{T} E_{\hat{\pi}}[c(\mathbf{x}_{t'}, \mathbf{u}_{t'})] + \lambda D_{\mathrm{KL}}(\hat{\pi}(\mathbf{u}_t | \mathbf{x}_t) || \pi_{\theta}(\mathbf{u}_t | \mathbf{o}_t))$
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 $\mathbf{v}_{t'} = \mathbf{v}_{t'} = \mathbf{v}_{t'} = \mathbf{v}_{t'} = \mathbf{v}_{t'=t'} \sum_{t'=t'}^{T} E_{\hat{\pi}}[c(\mathbf{x}_{t'}, \mathbf{u}_t] + \mathbf{v}_{t'}]$
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DAgger vs GPS

- DAgger does not require an adaptive expert
 - Any expert will do, so long as states from learned policy can be labeled
 - Assumes it is possible to match expert's behavior up to bounded loss
 - Not always possible (e.g. partially observed domains)
- GPS adapts the "expert" behavior
 - Does not require bounded loss on initial expert (expert will change)

Why imitate optimal control?

- Relatively stable and easy to use
 - Supervised learning works very well
 - Optimal control (usually) works very well
 - The combination of the two (usually) works very well
- Input remapping trick: can exploit availability of additional information at training time to learn policy from raw observations
- Overcomes optimization challenges of backpropagating into policy directly
- Usually sample-efficient and viable for real physical systems

Model-based RL algorithms summary

- Learn model and plan (without policy)
- THIS WILL BE ON HWA! Iteratively collect more data to overcome distribution mismatch
 - Replan every time step (MPC) to mitigate small model errors
- Learn policy
 - Backpropagate into policy (e.g., PILCO) simple but potentially unstable
 - Imitate optimal control in a constrained optimization framework (e.g., GPS)
 - Imitate optimal control via DAgger-like process (e.g., PLATO)

Limitations of model-based RL

- Need some kind of model
 - Not always available
 - Sometimes harder to learn than the policy
- Learning the model takes time & data
 - Sometimes expressive model classes (neural nets) are not fast
 - Sometimes fast model classes (linear models) are not expressive
- Some kind of additional assumptions
 - Linearizability/continuity
 - Ability to reset the system (for local linear models)
 - Smoothness (for GP-style global models)
 - Etc.





Which RL algorithm to use?

