

Cooperative Occlusion-Aware Multi-Robot Target Tracking using Optimization

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Abstract—We introduce an optimization-based control approach that enables a team of robots to cooperatively track a target using onboard sensing. In this setting, the robots are required to estimate their own positions as well as concurrently track the target. Our probabilistic method generates controls that minimize the expected future uncertainty of the target. Additionally, our method efficiently reasons about occlusions between robots and takes them into account for the control generation. We evaluate our approach in a number of experiments in which we simulate a team of quadrotor robots flying in three-dimensional space to track a moving target on the ground. We compare our method to other state-of-the-art approaches represented by the random sampling technique, lattice planning method, and our previous method. Our experimental results indicate that our method achieves 4 times smaller average maximum tracking error and 3 times smaller average tracking error than the next best approach in the presented scenario.

I. INTRODUCTION

Tracking a moving target has many potential applications in various fields. For example, consider a search and rescue scenario where autonomous ground robots are deployed to assist disaster victims but they are not able to localize themselves in an unknown environment. In this case, one could use flying robots that due to their higher altitude can take advantage of, e.g., GPS signals on the one hand and can help to localize the ground robots by observing them on the other hand. Although it comes at the cost of higher complexity in motion planning, using multiple cooperatively controlled robots in this setting provides undisputed advantages, such as increased coverage, robustness to failure and reduced uncertainty of the target.

Consider a scenario depicted in Fig. 1 where a team of aerial robots equipped with onboard cameras is tasked with tracking and estimating the position of a mobile robot with respect to a global frame of reference. Some of the quadrotors may be in the field of view of the external global sensor while others are not. The ideal cooperative control algorithm for this team would take into account all visibility constraints and uncertainties in order to establish a configuration of quadrotors that enables to propagate position information from the global sensors through the quadrotors to the target.

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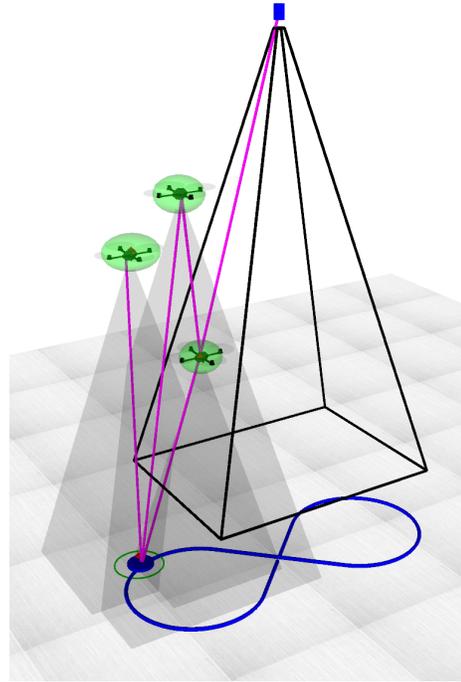


Fig. 1. Three quadrotors cooperatively tracking a target following a figure-eight trajectory (blue line). The green ellipsoids show the 3-dimensional covariances of quadrotors' positions. The green ellipse represents the 2-dimensional covariance of the position of the target. Magenta lines depict the measurements between quadrotors and the global camera (blue cube at the top). How should the quadrotors move in order to minimize the uncertainty of the target?

We introduce a centralized planning approach that generates controls for multiple robots and minimizes the uncertainty of the tracked target. At any particular instance an individual quadrotor may not be able to see the target due to occlusions or the sensor's limited field-of-view. To formulate a cost function that considers these discontinuities in the sensor domain, we extend the approach from [23] to multiple robots and penalize the trace of the target's covariance. Using this cost function, we employ an optimization framework to find locally optimal controls. We execute these controls and estimate the state of the quadrotor team and target using an Extended Kalman Filter (EKF) [27].

The novel contributions of this paper are as follows: a) we take into account sensing discontinuities caused, for example, by occlusions in different multi-robot configurations in a manner that is amenable to continuous optimization, and b) we generate controls in 3 dimensions for all the quadrotors, hence there is no need for additional reasoning about

potential multi-robot sensing topologies. We evaluated our approach in a number of simulations and compared it to our previous method in which we introduced cooperative multi-robot control with switching of sensing topologies [12].

II. RELATED WORK

The task of cooperative target tracking has been addressed in various ways. Many researchers considered centralized [6, 8], decentralized [1, 19, 21, 22], and distributed [16, 17, 28] approaches to control multiple aerial or ground robots. Nevertheless, all of the above approaches do not take into account the position uncertainty of the robots that are deployed to perform the tracking task. The position of the robots is assumed to either be known or independently obtained with high accuracy. In this work, we consider both, the position uncertainty of the tracked target as well as the uncertainty in the robots' poses, which effectively eliminates the need of a highly accurate external tracking system.

The problem of target localization is very similar to the task of target tracking. There have been many authors that worked on target localization [9, 10, 11, 13, 26] in a multi-robot scenario with onboard sensing. It is worth noting that these approaches are implemented in a distributed fashion which makes them well-suited for multi-robot scenarios with limited communication. One of the simplifications introduced in these approaches, however, is to limit the robots to planar movements and disable the possibility that the robots can be perceived by each other. In our work, we relax these assumptions and show how to cope with occlusions between different robots. Furthermore, the above-mentioned approaches use the mutual information measures as an uncertainty measure. In contrast, we use the trace of the covariance, which as shown by Beinhofer et al. [4] copes better with degenerate covariances.

Another tracking approach was proposed by Ahmad and Lima [2] where the authors weight the observations of individual robots based on their localization uncertainty. Zhou and Roumeliotis [29] proposed a similar approach but their focus is on the non-convex optimization of the cost function and evaluation of different sensor models. In both of these approaches, the authors decouple the target tracking from the robots' localization which results in not taking into account the high correlation of the target's and the robots' position estimates.

There have been several optimization-based approaches [3, 14, 15] that tackle the problem of cooperative multi-robot localization using only onboard sensors. These approaches, however, provide the maximum-likelihood state estimates which does not allow to directly minimize the uncertainty of the target pose.

In our previous work [12] we introduced the concept of level-based sensing topologies, which simplifies the reasoning about occlusions and reduces the considered control space of each robot to a two-dimensional plane. In this paper, we tackle the problem of generating locally optimal controls for each quadrotor in the full 3-dimensional space and we explicitly reason about occlusions in the trajectory

optimization algorithm. In addition, we do not, as previously, apply the same controls over the look-ahead horizon in the optimization but consider arbitrary trajectories with different controls for different time steps. Moreover, by removing the level-based sensing topologies in this work, we enable more realistic simulations as the quadrotors are not assumed to instantly jump from one topology level to another.

III. APPROACH

We propose a centralized approach where we jointly estimate the positions of the quadrotors and the target using an EKF. First, we describe our state estimation technique to then focus on the control generation and reasoning about occlusions.

A. State Estimation with EKF

1) *System Parametrization:* The state at time t consists of the individual quadrotor poses $\mathbf{x}_t^{(i)}$, $i \in [1, n]$ and the target pose $\mathbf{x}_t^{(target)}$. Let $\mathbf{u}_t^{(i)}$ be the control input applied to the i th robot at time t . The joint state and control input are defined as:

$$\mathbf{x}_t = [\mathbf{x}_t^{(1)}, \dots, \mathbf{x}_t^{(n)}, \mathbf{x}_t^{(target)}] \quad (1)$$

$$\mathbf{u}_t = [\mathbf{u}_t^{(1)}, \dots, \mathbf{u}_t^{(n)}] \quad (2)$$

Let Σ_t be the uncertainty covariance of the joint state.

The dynamics and measurement models for the joint state are given by the stochastic, differentiable functions \mathbf{f} and \mathbf{h} :

$$\mathbf{x}_{t+1} = \mathbf{f}(\mathbf{x}_t, \mathbf{u}_t, \mathbf{q}_t), \quad \mathbf{q}_t \sim N(\mathbf{0}, Q_t) \quad (3)$$

$$\mathbf{z}_t = \mathbf{h}(\mathbf{x}_t, \mathbf{r}_t), \quad \mathbf{r}_t \sim N(\mathbf{0}, R_t) \quad (4)$$

where \mathbf{q}_t is the dynamics noise, \mathbf{r}_t is the measurement noise, and they are assumed to be zero-mean Gaussian distributed with state-dependent covariances Q_t and R_t , respectively.

We consider two types of sensors and corresponding measurements: absolute (global) measurements, e.g., GPS, and relative measurements between two quadrotors or a quadrotor and the target, e.g., distance or relative pose measurements. The stochastic measurement function of the absolute sensors is given by:

$$\mathbf{z}_t^{(i)} = \mathbf{h}^{(i)}(\mathbf{x}_t^{(i)}, \mathbf{r}_t^{(i)})$$

while the relative sensor model is:

$$\mathbf{z}_t^{(i,j)} = \mathbf{h}^{(i,j)}(\mathbf{x}_t^{(i)}, \mathbf{x}_t^{(j)}, \mathbf{r}_t^{(i,j)})$$

All measurement functions can be naturally extended for the joint state [20].

2) *Uncertainty Model:* Given the current belief (\mathbf{x}_t, Σ_t) , control input \mathbf{u}_t and measurement \mathbf{z}_{t+1} , the beliefs evolve using an EKF.

In order to model the discontinuity in the sensing domain, which can be caused either by a limited field of view or occlusions, we follow the method from [23] and introduce a binary vector $\delta_t \in \mathbb{R}^{\dim[\mathbf{z}]}$. The k th entry in the vector δ_t takes the value 1 if the i th dimension of \mathbf{z}_t is available and a value of 0 if no measurement is obtained. We detail the method for computing δ_t in Sec. III-C.

The EKF update equations are as follows:

$$\mathbf{x}_{t+1} = \mathbf{f}(\mathbf{x}_t, \mathbf{u}_t, \mathbf{0}) + K_t(\mathbf{z}_t - \mathbf{h}(\mathbf{x}_t)) \quad (5a)$$

$$\Sigma_{t+1} = (I - K_t H_t) \Sigma_t^- \quad (5b)$$

$$K_t = \Sigma_{t+1}^- H_t^T \Delta_t [\Delta_t H_t \Sigma_{t+1}^- H_t^T \Delta_t + W_t R_t W_t^T]^{-1} \Delta_t \quad (5c)$$

$$\Sigma_{t+1}^- = A_t \Sigma_t A_t^T + V_t Q_t V_t^T \quad (5d)$$

$$A_t = \frac{\partial \mathbf{f}}{\partial \mathbf{x}}(\mathbf{x}_t, \mathbf{u}_t, \mathbf{0}), \quad V_t = \frac{\partial \mathbf{f}}{\partial \mathbf{q}}(\mathbf{x}_t, \mathbf{0}) \quad (5e)$$

$$H_t = \frac{\partial \mathbf{h}}{\partial \mathbf{x}}(\mathbf{x}_{t+1}, \mathbf{0}), \quad W_t = \frac{\partial \mathbf{h}}{\partial \mathbf{r}}(\mathbf{x}_{t+1}, \mathbf{0}), \quad (5f)$$

where $\Delta_t = \text{diag}[\delta_t]$ and \mathbf{z}_t is a measurement obtained at time step t .

It is worth noting that the Kalman gain update in Eq. 5c includes the binary matrix Δ_t to account for discontinuities in the sensor domains. Furthermore, we apply the Markov assumption [27] that the measurements are conditionally independent given the joint state. Thus, the individual measurements can be separately fused into the belief using the EKF update equations.

3) *Dynamics Model*: We assume that the orientation of the quadrotors is fixed and one can only control their 3D position. The dynamics of an individual quadrotor is given by: $\mathbf{f}^{(i)}(\mathbf{x}^{(i)}, \mathbf{u}^{(i)}, \mathbf{q}^{(i)}) = \mathbf{x}^{(i)} + \mathbf{u}^{(i)} \Delta t + \mathbf{q}^{(i)}$ where $\mathbf{x}^{(i)}, \mathbf{u}^{(i)} \in \mathbb{R}^3$ are the 3D position and velocity and Δt is the length of a time step. For modeling the target motion, one can apply a standard uncontrolled motion model. In this work, we assume a constant velocity motion model.

4) *Observation Model*: The cameras are assumed to be at the center of each quadrotor facing down. The absolute sensor provides the 3D position of the observed quadrotor/target as a measurement:

$$\mathbf{h}^{(i)}(\mathbf{x}_t^{(i)}, \mathbf{r}_t^{(i)}) = \mathbf{x}_t^{(i)} + \mathbf{r}_t^{(i)}$$

The relative sensor model provides the position of the (observed) j th quadrotor/target relative to the (observing) i th quadrotor:

$$\mathbf{h}^{(i,j)}(\mathbf{x}_t^{(i)}, \mathbf{x}_t^{(j)}, \mathbf{r}_t^{(i,j)}) = (\mathbf{x}_t^{(j)} - \mathbf{x}_t^{(i)}) + \mathbf{r}_t^{(i,j)}.$$

B. Control Generation using Optimization

At each time step t we seek a set of control inputs $\mathbf{u}_{t:T=t+h}$ that for a time horizon h minimizes the uncertainty of the target while penalizing collisions and the control effort. In order to minimize the uncertainty of the target, we, similarly to [4], penalize the trace of the target covariance. The other components included in the cost function are: the distance of every quadrotor pair to avoid collisions and the cost of the control effort. The final cost function is composed as follows:

$$c_t(\mathbf{x}_t, \Sigma_t, \mathbf{u}_t) = \alpha \text{tr}(\Sigma_t^{(target)}) + \beta c_{collision}(\mathbf{x}_t) + \gamma \|\mathbf{u}_t\|_2^2$$

$$c_T(\mathbf{x}_T, \Sigma_T) = \alpha \text{tr}(\Sigma_T^{(target)}) + \beta c_{collision}(\mathbf{x}_T)$$

$$c_{collision}(\mathbf{x}) = \sum_{i=1}^n \sum_{j=i+1}^n \max(\|\mathbf{x}^{(j)} - \mathbf{x}^{(i)}\|_2 - d_{max}, 0)$$

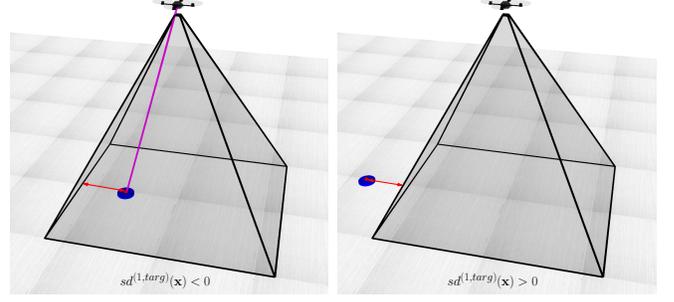


Fig. 2. Signed distance if the quadrotor/target is inside the view frustum (left) and outside the view frustum (right).

where α, β , and γ are user-defined scalar weighting parameters and d_{max} is the maximum distance for which the collision cost takes effect.

To eliminate the stochasticity of the cost functions, we follow Platt et al. [25] and assume the maximum likelihood observation is obtained at each time step. The final objective function is:

$$\min_{\mathbf{x}_{t:T}, \mathbf{u}_{t:T-1}} E[c_T(\mathbf{x}_T, \Sigma_T) + \sum_t^{T-1} c_t(\mathbf{x}_t, \Sigma_t, \mathbf{u}_t)] \quad (6)$$

$$\text{s. t. } \mathbf{x}_{t+1} = \mathbf{f}(\mathbf{x}_t, \mathbf{u}_t, \mathbf{0})$$

$$\mathbf{x}_t \in \mathcal{X}_{feasible}, \quad \mathbf{u}_t \in \mathcal{U}_{feasible}$$

$$\mathbf{x}_0 = \mathbf{x}_{init}, \quad \Sigma_0 = \Sigma_{init}$$

For trajectory optimization, one can solve a nonlinear optimization problem to find a locally optimal set of controls [24]. In this work, we used sequential quadratic programming (SQP) to locally optimize the non-convex, constrained optimization problem. The innermost QP solver was generated by a numerical optimization code framework called FORCES [7]. FORCES generates code for solving QPs that is specialized for convex multistage problems such as trajectory optimization.

Given the output controls $\mathbf{u}_{t:T-1}$ computed using trajectory optimization, we follow the model predictive control paradigm [5] by executing a subset of the optimized controls and then replanning. We use the previously computed controls as an initialization to warm start the optimization.

C. Reasoning about Oclusions

The absolute/relative position of a quadrotor/target may not be observable due to oclusions from other quadrotors and the limited field-of-view of the sensor. As previously mentioned, we model this discontinuity with the binary variable δ (according to [23]). In order to make the objective function differentiable, we approximate δ with a sigmoid function. It is worth noting that this is only required in the optimization step, the state estimation step remains as defined previously.

Let $\text{sd}^{(i,j)}(\mathbf{x})$ be the signed distance of $\mathbf{x}^{(j)}$ to the field-of-view of the i th quadrotor (see Fig. 2). The signed distance is negative if the j th quadrotor is visible and positive otherwise. We introduce the parameter α which determines the slope of the sigmoidal approximation. The sigmoidal

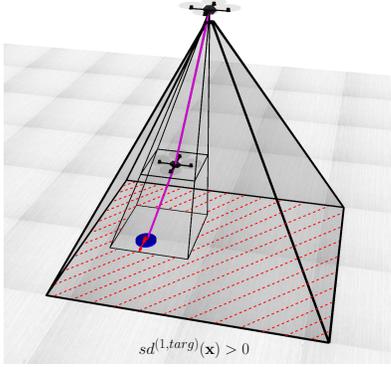


Fig. 3. Signed distance function in the presence of occlusions. First, we determine the shadows of all the occlusions such that the resulting field-of-view (the shaded area) is calculated. The signed distance is computed as the distance to the field-of-view.

approximation of the measurement availability δ is given by:

$$\delta^{(i,j)} = \frac{1}{1 + \exp[-\alpha \cdot \text{sd}^{(i,j)}(\mathbf{x})]} \quad (7)$$

For more details on the sigmoidal approximation of the availability of the measurement we refer the reader to [23].

To calculate the signed distance of $\mathbf{x}^{(j)}$ to the field-of-view of $\mathbf{x}^{(i)}$, we first represent the field-of-view as a truncated view frustum with a minimum and maximum distance given by the sensor model as depicted in Fig. 3. If $\mathbf{x}^{(j)}$ is outside of the view frustum, $\text{sd}^{(i,j)}(\mathbf{x})$ is the distance of $\mathbf{x}^{(j)}$ to the view frustum as shown in the right plot in Fig. 2. If $\mathbf{x}^{(j)}$ is inside the view frustum and there are no occlusions, the signed distance is computed as shown in the left plot in Fig. 2. In the presence of occlusions, we first determine the shadows of all the occlusions in the plane of $\mathbf{x}^{(j)}$. In the next step, we use an open source 2D polygon clipping library - GPC¹ to generate the 2D polygon field-of-view, and then calculate the signed distance. Fig. 3 shows an example of a signed distance function in the presence of an occlusion.

IV. EVALUATION AND DISCUSSION

We evaluated our approach in a number of simulation experiments. The simulation environment consists of a global down-looking camera attached 4 meters above the origin of the coordinate system, a ground robot target and a varying number of quadrotors equipped with down-looking cameras. Each quadrotor is controlled through the velocity commands $\mathbf{u}^{(i)} = [v_x, v_y, v_z]$. The state of the target consists of its position and velocity $\mathbf{x}^{(targ)} = [x, y, v_x, v_y]$ and the target moves on the XY-plane in a figure-eight trajectory (see Fig. 1). All camera sensors in this setup have the same properties and can detect objects in a 3-meter high truncated pyramid. Consequently, the global camera is not able to see the target directly. An example of a system setup with the field of view of each camera is depicted in Fig. 1. Our system aims to estimate the position of the target as accurately as possible by actively controlling the quadrotors.

A. Experiments

We present different sets of experiments illustrating various evaluation criteria of our system.

1) *Time Horizon Experiment*: We evaluate the influence of different time horizons on the tracking accuracy. Fig. 4 shows the statistics for three different time horizons. There is no significant difference between the three presented plots. This leads to a conclusion that larger time horizon factor in the optimization step has no significant influence on the effectiveness of our approach. This is most likely due to the challenging shape of the target trajectory. The optimization applies the constant velocity prediction of the target which is constantly violated by the fact that the target is turning to follow the trajectory. Based on these findings, we set the time horizon to be 2 for the remaining experiments.

2) *Sampling vs. Optimization Experiment*: We compare our optimization based control generation with random sampling [6] and lattice planners [18]. Random sampling methods randomly sample controls to generate trajectories while lattice planners draw samples from a predefined manifold, which in our case was a sphere with radius equal to the maximum allowed control effort. For both methods, the cost of each resulting trajectory is evaluated and the controls corresponding to the minimum cost trajectory are executed. Fig. 5 shows the statistical results of the comparison between the sampling method, lattice sampling method and our approach for 3 quadrotors. In order to make a fair comparison for the sampling methods, we chose the number of samples such that the execution times per one optimization step of all the methods were similar and we averaged the results over 10 runs. One can notice a significantly larger tracking error and the trace of the target covariance in performance of both of the sampling methods compared to the trajectory optimization approach. It is worth noting that the lattice approach yields worse results than the random sampling approach. It is most likely due to the fact that generating controls of the same magnitude throughout the trajectory causes the quadrotors to constantly overshoot the target. Given the constant velocity assumption, the challenging shape of figure eight appears to be too difficult to follow by using sampling approaches.

3) *Number of Quadrotors Experiment*: We compared the tracking performance and the execution time for different numbers of quadrotors. The statistics presented in Fig. 6 demonstrates a visible improvement by using a larger number of quadrotors which confirms the intuition that larger teams facilitate more reliable and accurate target tracking. It is important to note that the quadrotors are able to leverage their large quantity despite the very narrow field of view of the cameras. This behavior is achieved because of the reasoning about occlusions which prevents the quadrotors to block each other's views. In this experiment, similar to the other experiments, one can notice two bumps in the error statistics in the presented figures. These correspond to the ends of figure eight, where the quadrotors have to spread out in order to continue tracking the target, causing some of

¹<http://www.cs.man.ac.uk/~toby/gpc/>

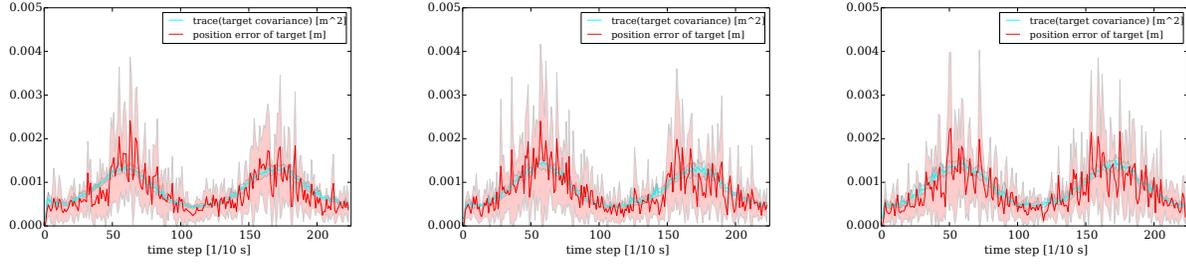


Fig. 4. Comparison of different time horizons in the optimization step. The time horizons are 2, 5, and 10, respectively. Evaluation measures are shown with 95% confidence intervals over 10 runs with 3 quadrotors. There is no significant difference in the tracking error for these time horizons.

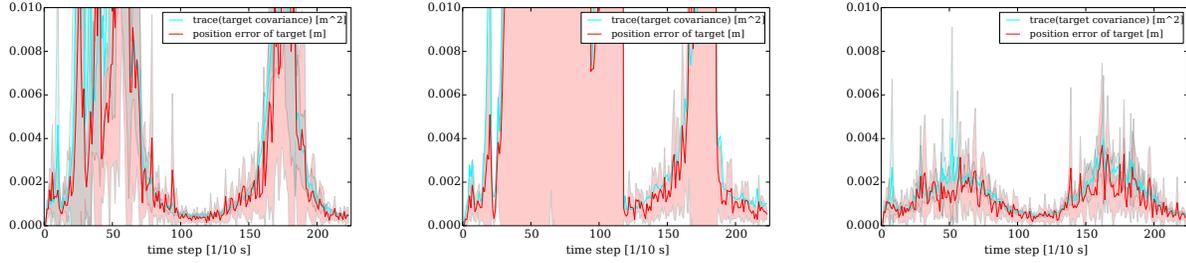


Fig. 5. Comparison between different sampling approaches and the optimization approach presented in this paper. From left to right: random sampling, lattice sampling and optimization. Evaluation measures are shown with 95% confidence intervals over 10 runs with 3 quadrotors. The optimization approach yields better results than the other presented methods.

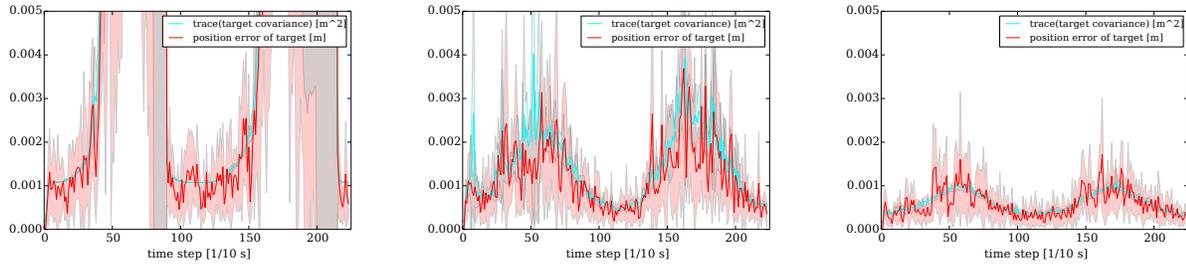


Fig. 6. Comparison of our optimization-based approach applied to different number of quadrotors used for the tracking task. From left to right the number of quadrotors are: 1, 3 and 5. Evaluation measures are shown with 95% confidence intervals over 10 runs. The experiments confirms the intuition that deploying more quadrotors improves the tracking performance.

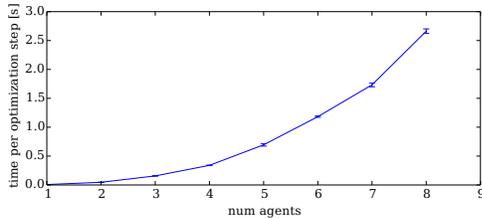


Fig. 7. Statistics over 10 runs of time per one optimization step for different number of quadrotors. Time per optimization step scales quadratically with the number of quadrotors.

the quadrotors to be temporarily outside the field-of-view of the global camera.

Fig. 7 depicts the average time for one optimization step for different numbers of quadrotors. The curve grows quadratically, which is expected, because of the n^2 number of potential observations that have to be evaluated for all the quadrotor pairs.

4) *Optimization with Occlusions Experiment:* To evaluate the importance of considering occlusions, we evaluated our method with and without reasoning about occlusions for a team of 3 quadrotors (Fig. 8) and measured the target covariance and target tracking error. Of note is the higher

uncertainty in Fig. 8(top) than Fig. 8(bottom) at the beginning, middle, and end of the target trajectory. When not considering occlusions, the error is higher at these segments because these segments are directly underneath the global camera, which leads to a crowded space. In this scenario, when not considering occlusions in the optimization, the quadrotors block each other's views, resulting in worse tracking error as compared to considering occlusions in the optimization.

5) *Topology Switching Experiment:* We compare the method proposed in this paper to our previous target tracking method that introduced level-based sensing topologies and an efficient topology switching algorithm [12]. In this approach, the quadrotors are organized on different levels with an assumption that each level can only sense the adjacent level below it. At each time step the algorithm determines the planar controls for each of the quadrotors as well as determines whether to switch to one of the neighboring topologies by moving one of the quadrotors by one level up or down. This approach was introduced in order to avoid the reasoning about occlusions between quadrotors at different altitudes. However, a topology switch is assumed to be instantaneously completed, which is not realistic.

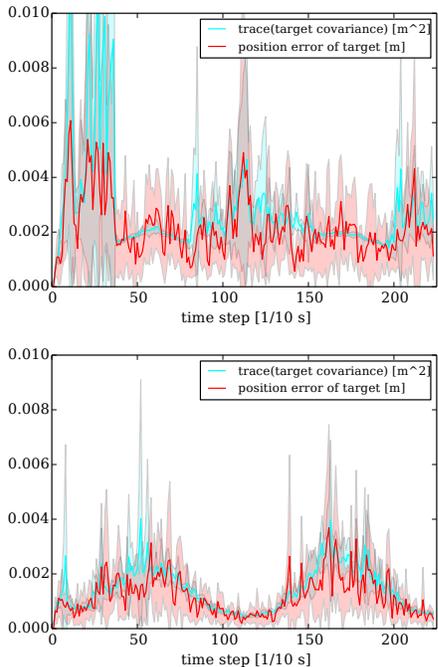


Fig. 8. Comparison between not taking occlusions into account in the optimization step (top) and accounting for occlusions using the signed distance function presented in this work (bottom). Statistics and 95% confidence intervals over 10 runs with 3 quadrotors. Taking occlusions into account is beneficial especially at the spots right below the global camera (i.e. start, middle and the end of the trajectory).

In order to make our approach and the level-based approach comparable for standard quadrotors, we introduce a length 3 time step delay for the topology switch in order to realistically simulate a real quadrotor adjusting altitude. The performance of both algorithms is depicted in Fig. 9. The quadrotors perform better when explicitly reasoning about occlusions with our approach, especially at the borders of the figure eight where the target is far away from the global camera. This phenomena can be explained by analyzing Fig. 10. In the level-based approach, if the target is far away from the global camera the optimal topology is a chain topology. Our approach, however, is able to form a different sensing topology that is superior to the previous one due to its higher number of available measurements (see Fig. 10). This superior topology is not valid for the level-based approach as it violates the assumption of sensing only the adjacent level below the current level. This topology enables the algorithm to localize the quadrotor on the left side due to the measurement of the other quadrotor and have two localized quadrotors observe the target. It is worth noting that our novel approach can create a greater variety of sensing topologies compared to our previous approach without explicitly reasoning about sensing topologies.

6) *Average Error Comparisons:* Table I shows the statistics of the average tracking error and maximum average tracking error for different approaches tested in our experiments. It is worth noting that our approach achieved 4 times smaller average maximum tracking error than the next best method, the level-based approach. Our method also achieves

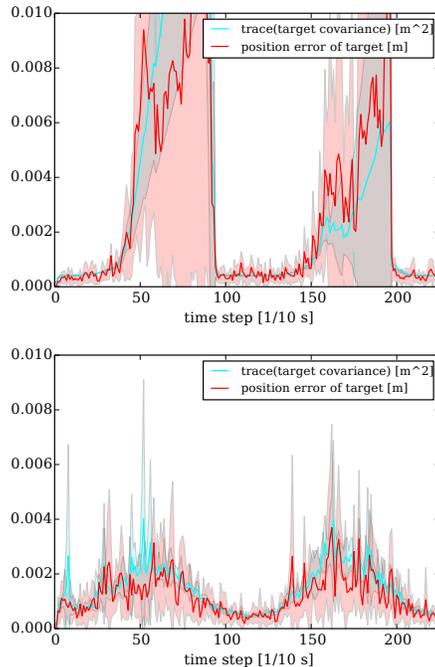


Fig. 9. Target tracking results for our previous level-based approach [12] (top) and the hereby presented method without explicitly reasoning about sensing topologies (bottom). Statistics and 95% confidence intervals over 10 runs with 3 quadrotors. The approach presented in this paper is more beneficial for the reasons explained in Fig. 10.

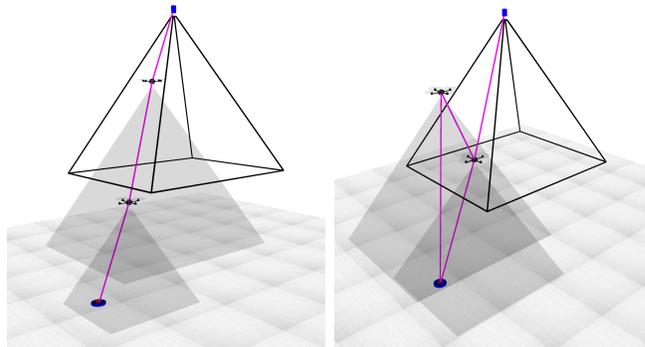


Fig. 10. An example of an advantage of our approach over the level-based approach. Left: most beneficial sensing topology for the level-based approach. The quadrotors form a chain topology as each level of quadrotors is allowed to sense only one level below it. Right: A superior sensing topology achieved by our novel method. The lower quadrotor is seen by the global sensor and the other quadrotor. The upper quadrotor can localize itself based on the observation of the lower quadrotor. Both quadrotors can observe the tracking target which provides more information than the level-based approach. There are no constraints for the topology levels.

a 3 times smaller average tracking error compared to the level-based approach.

V. CONCLUSIONS AND FUTURE WORK

We presented an optimization-based probabilistic multi-robot target tracking approach that efficiently reasons about occlusions. We evaluated our approach in a number of simulation experiments. We have compared our method to other baseline approaches such as random sampling, lattice sampling, and our previous work on sensing topologies [12]. Our experimental results indicated that our method achieves

	level-based 2D optimization	lattice planning	random sampling	our approach (3D optimization)
average max tracking error [m]	0.0156 ± 0.024	0.41 ± 1.00	0.027 ± 0.028	0.0037 ± 0.005
average tracking error [m]	0.0030 ± 0.0036	0.037 ± 0.073	0.0035 ± 0.0044	0.0012 ± 0.0007

TABLE I. Quantitative results for the experiments with 3 quadrotors. Max target tracking error was averaged over 10 runs, target tracking error was averaged over all time steps and 10 runs. Our approach yields significantly smaller error than the other baseline methods.

4 times smaller average maximum tracking error and 3 times smaller average tracking error than the next best approach in the presented scenario.

In future work, we plan to extend our centralized planning approach to fully decentralized, distributed planning. This is advantageous in multi-robot settings with limited communication. Finally, we would like to further demonstrate the applicability of our approach in a real robot scenario.

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